Designing the raw material collection system for profit maximization under a step–price policy

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Abstract

In this study, we investigate a complex situation in designing a raw material collection system, which involves collection station location, supplier selection, supplier–collection allocation, and transportation decisions. In a raw material collection system, a collector has to collect more raw material quantity in order to get higher income as the price of raw material is quantity dependent. The more suppliers visit, the more income receives; however, when a collector decides to visit more suppliers, traveling distance will be longer, which will result in higher transportation costs. We formulate a Mixed Integer Programming for a location routing with step–price policy model to find the optimal solution. The basic trade–off of the proposed model is between revenue received from totally collected quantity and total costs both fixed costs and variable costs from expanding the collection area. Instances which are created according to real–life data are applied to test the proposed model. The computational results indicate that the complex raw material collection system can be obtained by the proposed mathematical model. The mathematical model gives the benefit for the use of determining the optimum raw material collection system with profit maximization. The results can be used for setting up a real raw material collection system.

Keywords: location allocation, vehicle routing, profit maximization, step–price, price–quantity dependent

1. Introduction

Raw material collection systems are an important part in a supply chain of the agricultural industry where attention needs to be paid. When considering a raw material collection system in the agricultural industry, the collection process appears to be the main activity in the system. The logistics costs are a huge portion in the costs of the overall collection system. Most of the logistics costs, both fixed costs, such as collection station fixed costs, and variable costs, like transportation costs, rely on the operation model of a raw material collection system. In addition to these, the agricultural industry has specific characteristics such as perishable product that affects collection time and incentive system, which influences collected quantity, which is also needed to be considered when setting up a raw material collection system.

Similar to the distribution system, the important factors in designing a raw material collection system are locating facilities, such as collection stations and factories, allocating suppliers or customers to each service area, and transport plans covering all members in the system. For the aspect of collection stations, the location and the number of collection stations are both main factors in designing the collecting system, because changing the number of collection stations affects the supply chain cost as revealed by Chopra...
(2003). In the aspect of the allocation of suppliers to collection stations, the decision of assigning a supplier to each collection station is the main factor to be considered in the inbound collecting system design. Suppliers should be assigned to a proper collection station. For the transportation aspect, the number of suppliers selected in the route and the number of vehicles used in the routing are key factors that should be investigated for the design of an inbound collecting system. A vehicle needs to visit suppliers in the route and returns to the collection station under the capacity of the vehicle and within biological time constraints. In addition to the aforesaid factors, different sets of suppliers yield difference in revenues due to price–quantity dependencies, which makes a difference in the system costs. For the supplier selection aspect, the set of suppliers selected into a raw material collection system is vital factor that should be examined. One of the practical examples is the selecting of contracted suppliers for a contract farming system. Therefore, to establish such a complicated raw material collection system, it is necessary to involve not only the location decisions but also the allocation decision and routing decision, which should be determined, and the supplier selection decision that should be examined as well.

An integrated problem between a location problem and a routing problem, which is such a type of problem that deals with multi–functional problems, has been widely studied in supply chain management. Many studies (Laporte, 1988; Srivastava, 1993; Min et al., 1998; Tuzun and Burke, 1999; Wu et al., 2002; Ambrosino and Scutellà, 2005) have pointed out that the location routing problem (LRP) is defined as a vehicle routing problem in which the optimal number and locations of the depot are to be determined simultaneously with the vehicle schedules and the distribution routes so as to minimize the total costs. The location routing problem can be stated as following: given a feasible set of potential depot sites and customer sites, find the location of the depots and the routes to customers from the depots such that the overall cost of depot location and good distribution is minimized.

For the last two decades, many location allocation and vehicle routing models have been proposed (e.g. Min et al., 1998; Nagy and Sallie, 2007). Each model is characterized by the number of facilities to locate (single facility or multiple facilities), by the capacity constraints (facility capacity or vehicle capacity), by other route constraints (time windows or route length), and by the form of the objective function (cost minimization or profit maximization). Given a set of suppliers or customers, most studies have extensively developed models so as to minimize the total system costs in the range of various complicated environments, such as multiple hierarchical structure (Ambrosino and Scutellà, 2005), multiple vehicle types (Wu et al., 2002), demand in stochastic situation (Chan et al., 2001; Liu and Lee, 2003), and planning in dynamic case (Nambar et al., 1981; Ambrosino and Scutellà, 2005). Rarely does research address the profit maximizing problem. This research model hence undertakes other viewpoints by introducing the step–price policy in the model. With step–price environment, different quantity levels give different raw material prices. Therefore, it is essential to find a set of suppliers included in the raw material collection system. The purpose of this research is to find a solution for the problem of setting up a raw material collection system with step–price condition. With the holistic view model that considers step–price condition together with vehicle capacity and time duration restrictions, the optimal collection system needs to be found. The solution of the developed model is the strategy used for a raw material collection system set up by determining the location and the number of collection stations that need to be opened, a set of suppliers included into the system and the allocation of selected suppliers to each collection station, and a set of preliminary routes referring to the number of vehicles. This research emphasizes on the maximization of profit from raw material collection, which interrelates with the revenue from collected supply and total system costs.

The organization of this paper is as follows: The raw material collection system design problem with step–price policy condition is introduced in Section 2. The mathematical model formulated the investigated design problem is presented in Section 3. Some computational results are provided in Section 4. Finally, the conclusion of this study and future research development is discussed in Section 5.

2. Design Problems of a Raw Material Collection System

In view of today's management of raw material collection station, there are two stages of collector decision. The first stage is responsible for making set–up decisions, while the second stage is making operation decisions. For set–up decisions, the decision maker considers the location decision, supplier selection decision, allocation decision, and transportation decision. Given the set–up system mechanism, the operation decision is concerned on daily implementation related to transportation decision only. It means that by given a set of open collection stations and a set of selected suppliers, the reassignment of routing to collect raw material is determined. In this research, the designing of a raw material collection system in order to set up a proper collection system is studied. The collection system investigated consists of a number of suppliers, multiple collection stations with unlimited stocking area, and one factory the collected raw material has to be sent to.

In the system considered, raw material is collected from suppliers and then transported to the factory through the collector system. All collection stations have unlimited area for the stocking of raw material before transporting the collected raw material to the factory. This implies that each collection station can serve as many suppliers as the collector desires. In this research, only a single raw material is considered in the collection system. This means that only one identical product is produced by suppliers and collected by the collector. Raw material transportation is divided into two levels. The first level is the transportation between the
For the first level, identical vehicles with limited material handling capacity are dispatched from a collection station to visit a set of suppliers in order to collect raw material. Each collection station has its own vehicles for the collecting from suppliers and the transportation of raw material to collection stations. When the collection process is completed, the vehicle will return to its collection station. The collected raw material is then unloaded and prepared to delivery to the factory. In the raw material collection, we assume that the supplier is visited only once by one vehicle. The number of vehicles available at each collection station is unlimited. Irrespective of the number of vehicles needed for raw material collection, the collector can support them. There is one truck per one route; therefore, the number of trucks is equal to the number of routes. The transportation here is assumed to contract to a third party for picking up the raw material. The example trucks can be rented from car rental partner. The transportation costs here include both the vehicle fixed costs and the routing costs.

For the second level, larger vehicles will transport collected raw material directly from each collection station to the factory. The transportation between the collection station and the factory is assumed to subcontract to the transporter such as a logistics partner. The transportation cost here is charged for total collected quantity delivering from each particular collection station to the factory. Figure 1 gives an illustration of the raw material collection system investigated in this research.

Due to relatively larger demand than supply, most factories have incentive policies for their collectors so as to facilitate more supply quantities to the factories. One of the incentive policies, which are used in a raw material collection system, is the 'step–price policy' as example presented in Figure 2. Generally, in a collection system, the raw material price at each collection station is always based on the market price while raw material price at the factory varies according to step–price quantity levels. In this study, all collection stations pay suppliers with the same raw material price. The step–price quantity levels and step–prices offered to the collector are created by the factory. For example, if the raw material price at collection station is $p_0$ and $q^*$ is the collected quantity, and if $q_0 < q^* \leq q_1,$ then the raw material price at the factory is $p_1,$ but if $q_1 < q^* \leq q_2,$ then the price of raw material at the factory is $p_2,$ which is equal to $p_1$ plus any incentive price. Therefore, from a collector’s viewpoint, when the buying price ($p_0$) is fixed and the selling price per unit (step–price) is varied, a collector has to collect more raw material quantity in order to receive a higher price for the raw material at the factory.

With a step–price policy condition, it has to be a trade–off between revenue received from totally collected quantity and total costs, both fixed costs and variable costs, from expanding the collection area, if we want to get a higher step–price level. Because each set of suppliers yields different collected quantity resulting in different revenue; therefore, the set of suppliers included in the system is an essential point for designing a raw material collection system.

Moreover, the system considered here includes time duration and vehicle capacity constraints. Since the raw material, an agricultural product, is perishable quality of raw material can decay quickly. The collection process should be kept within biological time duration relevant to the perishability of the raw material. Not only biological time duration but also the vehicle capacity can limit the collection process. For example, if the capacity of vehicle is full, the vehicle has to return to the collection station.

In the situation of study, no shortage or delay occurs for the collection of raw material at any supplier’s point. It is assumed that every supplier has responsibility of getting raw material to the collection station.
material ready for picking up at any time. Furthermore, there is no inventory consideration in this research. Consequently, in order to maximize profit of the raw material collection system, a collector must decide where to collect raw material from and the number of suppliers, how many collection stations and where they should be located, how many vehicles in the system, and what routes each vehicle should take. A collector has to trade off between revenue from collected supply and total system costs, which include both fixed costs and variable costs, for the set–up of the raw material collection system under vehicle capacity, time duration and step–price policy circumstances.

3. Model Formulation

In the development of the location allocation and vehicle routing models, flow formulations have appeared to be the most widely used (Or and Pierskalla, 1979; Nambiar et al., 1981; Perl and Daskin, 1985; Bookbinder and Reece, 1988; Laporte, 1988; Aykin, 1995; Hansen et al., 1994; Albareda-Sàmbola et al., 2005; Ambrosino and Scutellà, 2005). Laporte (1988) has pointed out some mathematical models distinguishing between three–index and two–index location and routing flow formulations. Hansen et al. (1994) have modified the integer linear programming formulation of Perl and Daskin (1985) in order to provide an improved formulation, based on flow variables and flow constraints.

3.1 Mathematical model

The model investigated in this study is extended from the basic model of location allocation and vehicle routing problem by considering the selection of supplier. The aim of the model is to optimize raw material collection system in which the profit throughout the system is expected to maximize. The mathematical model is developed by location and routing models mentioned in Nambiar et al. (1981), Wu et al. (2002), and Ambrosino and Scutellà (2005). Some formulations are based on flow formulations provided by Laporte (1988); furthermore, step function formulations expressed in Tsai (2007) are also added. In order to formally state the problem, the notation, which will be used throughout the paper is introduced as following:

Sets:
- \( I \) represents the set of possible suppliers
- \( J \) represents the set of potential collection stations
- \( V \) represents the set of vehicles
- \( T \) represents the set of step–prices
- \( N \) represents the set of nodes, whereby \( N = I \cup J \)

Parameters:
- \( C_j \) represents the fixed cost of collection station \( j \), \( j \in J \)
- \( \beta \) represents the fixed cost of vehicle used between collection station and supplier
- \( h_j \) represents the transportation cost per unit quantity between collection station \( j \) and factory, \( j \in J \)
- \( r_{gh} \) represents the transportation cost between node \( g \) and node \( h \), \( g, h \in N \)
- \( p_0 \) represents the raw material price per unit quantity at collection station
- \( p_s \) represents the raw material price per unit quantity at factory at step–price \( s \), \( s \in T \)
- \( s_i \) represents the supply of supplier \( i \), \( i \in I \)
- \( q_s \) represents the minimum quantity level at step–price \( s \), \( s \in T \)
- \( e_{ij} \) represents the vehicle \( k \) set by collection station \( j, k \in V \), \( j \in J \)

where \( e_{ij} = 1 \) if vehicle \( k \) is set by collection station \( j \); otherwise \( e_{ij} = 0 \)
- \( L \) represents the capacity of vehicle used between collection station and supplier
- \( o_{gh} \) represents the traveling time between node \( g \) and node \( h \), \( g, h \in N \)
- \( a_i \) represents the loading time at supplier \( i \), \( i \in I \)
- \( B \) represents the biological time duration related to the perishability of raw material

Decision variables:
- \( y_{js} \) represents quantity sold at step–price \( s \), \( s \in T \)
- \( f_{ghk} \) represents quantity transported from node \( g \) to node \( h \) with the vehicle \( k \), \( g, h \in N \), \( k \in V \)
- \( w_j \) represents 1 if collection station \( j \) is opened, \( j \in J \); 0 otherwise
- \( z_i \) represents 1 if supplier \( i \) is included in the system, \( i \in I \); 0 otherwise
- \( u_s \) represents 1 if step–price \( s \) is chosen, \( s \in T \); 0 otherwise
- \( x_{ghk} \) represents 1 if an arc from node \( g \) to node \( h \) is on the route of vehicle \( k \), \( g, h \in N \), \( k \in V \); 0 otherwise

The model of location allocation and vehicle routing with step–price policy problem can be formulated as follows:

\[
\text{Max} \sum_{s \in T} \sum_{j \in J} p_s y_{js} - (p_0 \sum_{s \in T} \sum_{j \in J} f_{ghk} + \sum_{s \in T} \sum_{j \in J} w_j + \beta \sum_{s \in T} \sum_{j \in J} p_s + \sum_{s \in T} \sum_{j \in J} p_s x_{ghk}) = z_i \]

Subject to

\[
\sum_{s \in T} y_{js} = \sum_{s \in T} s z_i \quad \forall s \in T
\]

\[
q_s u_s \leq y_{js} \leq q_s u_s \quad \forall s \in T
\]

\[
\sum_{s \in T} u_s = 1
\]

\[
\sum_{h \in N} \sum_{s \in T} x_{ghk} = z_i \quad \forall i \in I
\]
The objective function (1) aims at maximizing the profit of the raw material collection system, which is the revenue from raw material collection minus the sum of raw material buying cost, collection station fixed cost, vehicle fixed cost, transportation cost between collection station and supplier, and transportation cost between collection station and factory. In constraints (2), total quantity sold at step–price \( s \) is equal to total collected quantity from selected suppliers. The constraints (3) enforce quantity sold at step–price must be in its step–price quantity level. The constraints (4) assure that only one step–price is selected. This implies that only one quantity level is chosen. To ensure only selected suppliers will be visited only once by one vehicle, the constraints (5) and (6) are added. Flow conservation constraint is expressed in constraints (7). This indicates that if a vehicle arrives at the node, it will leave that node. The constraints (8) guarantee that vehicle departs only from open collection stations. In constraints (9) and (10), a vehicle will leave and return to its own collection station. Moreover, these constraints ensure that each vehicle will leave from its own collection station mostly once. The constraints (11) state that the amount of quantity transported from the supplier is equal to the amount of quantity received by that supplier plus its own supply. The constraints (12) represent the subtour elimination constraint. This specifies that the quantity flows out from the supplier’s point must not be lower than the quantity flows at the supplier’s point. In capacity constraints (13), the collected quantity must not be larger than the capacity of vehicle. The constraints (14) make sure that travelling time in the route of vehicle and loading time of all suppliers allocated in that route must not exceed the biological time. The constraints (15) and (16) restrict variables \( y_s \) and \( f_{ghk} \) to non–negativity. Finally, the constraints (17) to (20) force variables \( w_j, z_i, u_s \) and \( x_{ghk} \) to binary, respectively.

### 3.2 Numerical example

Two potential collection stations, two possible suppliers and two step–prices are provided for verifying the mathematical model (Table 1 and Table 2). To verify the mathematical model, the numerical example is solved with the use of mathematical model by the AMPL/CPLEX solver and compared to the total enumerations method, which is the solving for all possible cases of problem solution. The results from mathematical model method (Table 3) report the same optimal solution with maximum profit as received from total enumerations method (Table 4).

### 4. Computational Results

In this section, we solve the proposed model with the goal of computing the optimum solution. To investigate the practical complexity of the proposed model, we use test sets of 9 instances. The instances differ for the number of collection stations to locate and for the number of suppliers to select. Locations of suppliers, collection stations, and the factory are generated in uniformly distribution in the range of \([0, 200]\). The number of potential collection stations and the number of possible supplier are varied from 2 to 5 and from 10 to 20, respectively. The supply from suppliers is generated in the interval \([100, 250]\). The fixed cost of collection station is generated in the interval \([20, 50]\). The vehicle fixed cost is given at \(25\). The unit transportation cost between supplier and collection station is varied in \([0.25, 0.5]\). Raw material price at collection stations and raw material step–prices at the factory are set as presented in Table 5.

<table>
<thead>
<tr>
<th>Node</th>
<th>Coordinate X</th>
<th>Coordinate Y</th>
</tr>
</thead>
<tbody>
<tr>
<td>Supplier #1</td>
<td>1</td>
<td>72</td>
</tr>
<tr>
<td>Supplier #2</td>
<td>89</td>
<td>158</td>
</tr>
<tr>
<td>Collection station #1</td>
<td>58</td>
<td>89</td>
</tr>
<tr>
<td>Collection station #2</td>
<td>29</td>
<td>30</td>
</tr>
<tr>
<td>Factory</td>
<td>84</td>
<td>39</td>
</tr>
</tbody>
</table>

The capacity of each vehicle used between the supply and collection station is generated a value no greater than 1,000.
The biological time is no greater than 5,000. Traveling time per distance is set as 1, and loading time per quantity is set as 0.025.

The Mixed Integer Programming (MIP) problem is solved by AMPL/CPLEX solver and run on PC with an Intel Core\textsuperscript{TM} 2 duo 2.33 GHz CPU and 1.96 GB of RAM. For each instance, in Table 6 we report the CPU time (in seconds) and the profit of optimal solution.

Table 2. Parameters used in the numerical example.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Supply of supplier #1</td>
<td>kg</td>
<td>164</td>
</tr>
<tr>
<td>Supply of supplier #2</td>
<td>kg</td>
<td>251</td>
</tr>
<tr>
<td>Fixed cost of collection station #1</td>
<td>Baht</td>
<td>42</td>
</tr>
<tr>
<td>Fixed cost of collection station #2</td>
<td>Baht</td>
<td>38</td>
</tr>
<tr>
<td>Transportation cost (Station #1 &amp; Factory)</td>
<td>Baht/kg</td>
<td>0.112712</td>
</tr>
<tr>
<td>Transportation cost (Station #2 &amp; Factory)</td>
<td>Baht/kg</td>
<td>0.111463</td>
</tr>
<tr>
<td>Transportation cost (Station &amp; Supplier)</td>
<td>Baht/km</td>
<td>0.25</td>
</tr>
<tr>
<td>Raw material cost at step–price 1</td>
<td>Baht/kg</td>
<td>2</td>
</tr>
<tr>
<td>Raw material quantity at step–price 1</td>
<td>kg</td>
<td>(124.5 &lt; Q &lt; 207.5)</td>
</tr>
<tr>
<td>Raw material cost at step–price 2</td>
<td>Baht/kg</td>
<td>2.25</td>
</tr>
<tr>
<td>Raw material quantity at step–price 2</td>
<td>kg</td>
<td>(207.5 &lt; Q)</td>
</tr>
<tr>
<td>Raw material buying cost at station</td>
<td>Baht/kg</td>
<td>1.75</td>
</tr>
<tr>
<td>Loading time per quantity</td>
<td>minute/kg</td>
<td>0.025</td>
</tr>
<tr>
<td>Traveling time per distance</td>
<td>minute/km</td>
<td>1</td>
</tr>
<tr>
<td>Biological time</td>
<td>minute</td>
<td>1000</td>
</tr>
<tr>
<td>Fixed cost of vehicle</td>
<td>Baht</td>
<td>32</td>
</tr>
<tr>
<td>Capacity of vehicle</td>
<td>kg</td>
<td>500</td>
</tr>
</tbody>
</table>

Baht – Thai monetary unit

Table 3. Results from the solution by the mathematical model method.

<table>
<thead>
<tr>
<th>Collection station</th>
<th>Route</th>
<th>Total distance</th>
<th>Total load</th>
<th>Total time</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>S1-1-2-S1</td>
<td>258.1697</td>
<td>415</td>
<td>268.5447</td>
</tr>
</tbody>
</table>

Table 4. Result from the solution by the total enumerations method.

<table>
<thead>
<tr>
<th>No.</th>
<th>Collection station</th>
<th>Supplier</th>
<th>Route</th>
<th>Profit</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
<td>1</td>
<td>S1-1-S1</td>
<td>-81.225</td>
</tr>
<tr>
<td>2</td>
<td>1</td>
<td>2</td>
<td>S1-2-S1</td>
<td>-14.612</td>
</tr>
<tr>
<td>3</td>
<td>1</td>
<td>12</td>
<td>S1-1-S1S1-2-S1</td>
<td>19.163</td>
</tr>
<tr>
<td>4</td>
<td>1</td>
<td>12</td>
<td>S1-1-2-S1</td>
<td>22.183</td>
</tr>
<tr>
<td>5</td>
<td>2</td>
<td>1</td>
<td>S2-1-S2</td>
<td>-72.518</td>
</tr>
<tr>
<td>6</td>
<td>2</td>
<td>2</td>
<td>S2-2-S2</td>
<td>-43.159</td>
</tr>
<tr>
<td>7</td>
<td>2</td>
<td>12</td>
<td>S2-1-S2S2-2-S2</td>
<td>-4.677</td>
</tr>
<tr>
<td>8</td>
<td>2</td>
<td>12</td>
<td>S2-1-2-S2</td>
<td>12.522</td>
</tr>
<tr>
<td>9</td>
<td>12</td>
<td>12</td>
<td>S1-1-S1S2-2-S2</td>
<td>-51.384</td>
</tr>
<tr>
<td>10</td>
<td>12</td>
<td>12</td>
<td>S1-2-S1S2-1-S2</td>
<td>-14.022</td>
</tr>
</tbody>
</table>

Table 6 shows that the optimum solution that has been obtained from the computing. The results report that the complex raw material collection system can be determined by the proposed mathematical model. Nevertheless, when solving large instances, CPLEX spends the majority of its time computing, and this time grows with the size of the instances. For instance, the set of test instances 4 require 386,028.6 seconds.
5. Conclusion

This research develops a mathematical model for an integrated location allocation and vehicle routing problem with step–price policy that is faced with the real–life situation in raw material collection and also useful for the operation research community. The location and the number of collection stations, a set of selected suppliers and the allocation of selected suppliers to collection stations, as well as a set of preliminary routes referring to the number of vehicles and to maximize the profit of the system are investigated in this study. The determination of an optimum raw material collection system is conducted under the consideration of price–quantity dependence, capacity of vehicle, and collection time duration. The mathematical model is beneficial for the use of determining the optimal raw material collection system with profit maximized criterion under the extension of step–price policy environment. It can be used for both single and multiple step–prices. For single step–price, the problem will turn to minimize system cost instead of profit maximization. The collector can apply the results for setting up of a raw material collection system. Generally, the integrated location allocation and vehicle routing MIP models are very large so that solvers are incapable of obtaining optimal solution in an acceptable computational time. The model developed then might solve to optimality but consume much time. Therefore, further research is needed to extend the application of heuristic approaches, such as multi–exchange neighborhood structures, which can effectively solve larger or more real–life problems to near optimality within a reasonable computational time.

References


